Cognitive and Noncognitive Factors in Educational Production

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Questions

This research examines the **joint effects of cognitive and noncognitive skills** on **academic achievement**.

→ What are the relative contributions of cognitive and noncognitive skills to academic performance, as measured by standardized test scores?

→ To what extent can noncognitive skills substitute for cognitive skills in producing academic outcomes, and how does this vary across subjects and genders?

→ Which type of skill improvement (cognitive or noncognitive) has a greater impact on grades, and does this differ between subjects like Maths and English?

Introduction

- **Context**: Irish secondary students, using Growing Up in Ireland longitudinal study data.
- **Methodology**: linear and translog production functions.
- **Main contribution**: Translog production function analysis of cognitive and noncognitive skills in academic achievement.
- **Key insights:**
  - Non-linear relationships and varying substitution elasticities across subjects and genders
  - Nuanced view of skill complementarity and substitutability
  - Optimization of human capital formation and resource allocation
  - Gender gap implications in educational strategies
- **Impact**: Informs targeted interventions and policies, emphasizing personalized approaches to human capital development.

Data and Model Specification

Data: Growing Up in Ireland longitudinal study (Waves 2 & 3, '98 Cohort)

Main Equation:

$$\text{Points\_JC}_{i,w,l} = \beta_0 + \beta_C \cdot \text{Cognition}_{i,w} + \sum_{j=1}^{J} \beta_{Nj} \cdot \text{NonCognition}_{i,w,k,j}$$

$$+ \sum_{j=1}^{J} \gamma_j \cdot (\text{Cognition}_{i,w} \cdot \text{NonCognition}_{i,w,k,j}) + \boldsymbol{\delta}' \cdot \textbf{Controls}_{i,w} + \varepsilon_{i,w,l,k,j}$$

Key Components (independent vars are z-distributed):

- **DV**: Junior Cert scores (Maths, English)
- **Cognitive Ability**: Principal Component (Naming, Maths, Vocabulary)
- **Noncognitive Measures**: SDQ (behavioural and emotional skills: Emotional Resilience, Good Conduct, Focused Behaviour Positive Peer Relationships), TIPI (personality traits: Agreeableness, Conscientiousness, Emotional Stability, Extroversion, Openness)
- **Controls**: SES, parental education, income, school characteristics
- Indices: i: individual, w: Wave, l: Subject, k: Caregiver, j: Noncognitive measures

Timeline

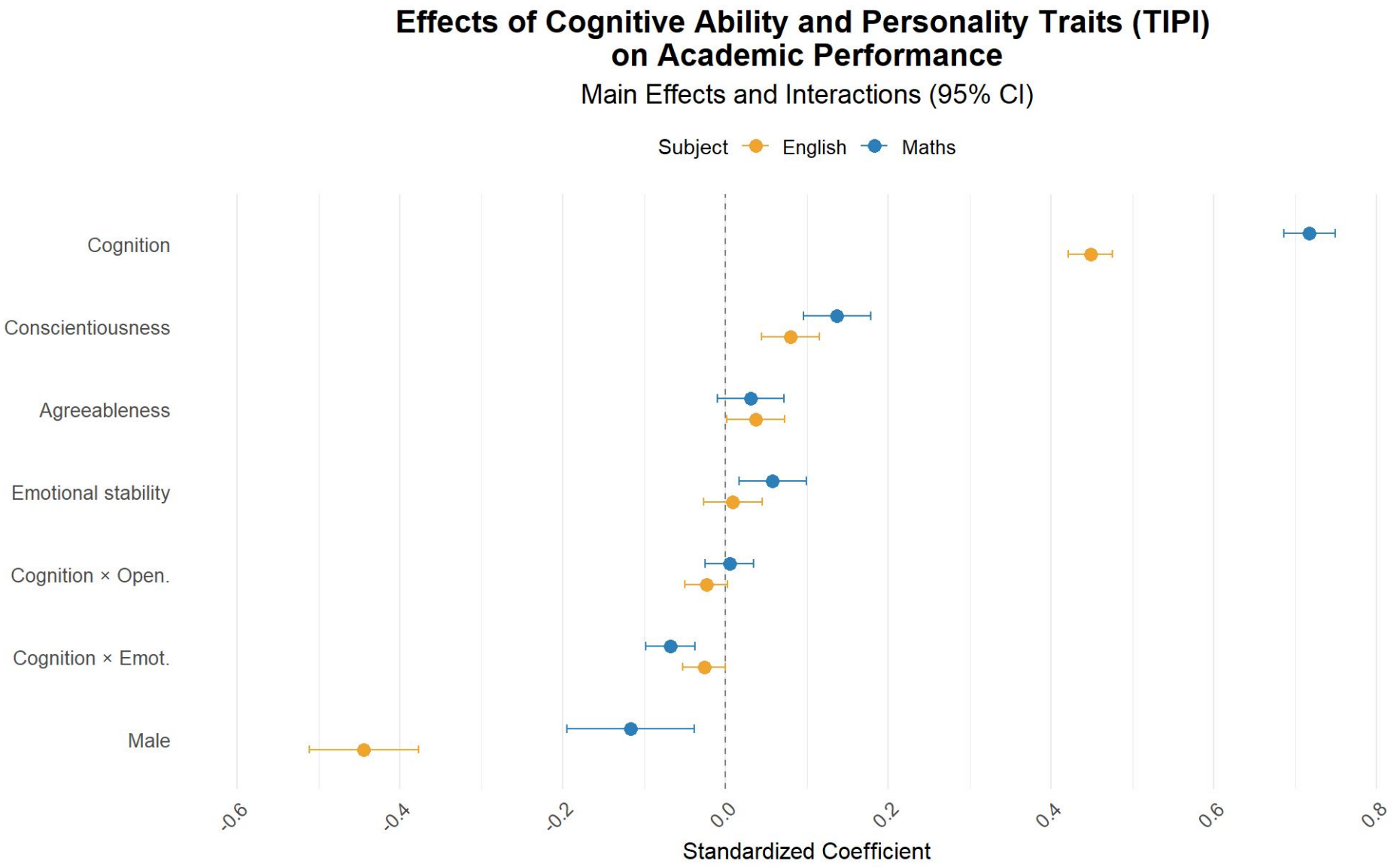
Timeline:

Event	Date	Age (in years)	Variables of interest
Study-child is born	Nov/97 - Oct/98	0	
Wave 2 data collection	Aug/11 - Mar/12	13	Independent variables: Cognition composite, SDQ and TIPI scales, controls
Study-child sits the Junior Cert	Jun/13 - Jun/14	15-16	
Wave 3 data collection	Apr/15 - Aug/16	17-18	Dependent variables: Junior Cert scores in Maths and English

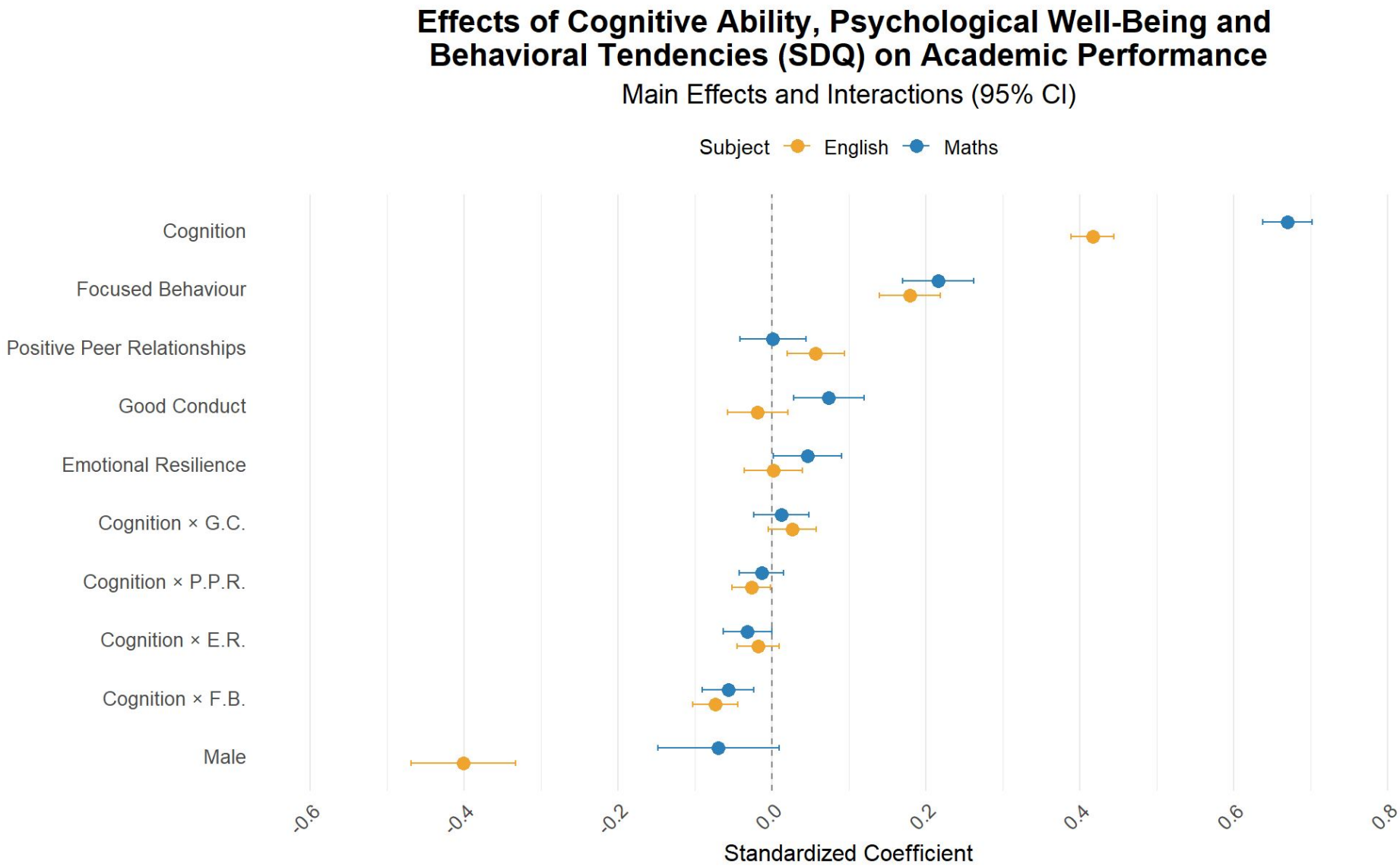
Table: Timeline of Events - Growing Up in Ireland '98 Cohort

Main Variables | Control Variables | Notes I | Notes II

Resuts - Linear Estimation - TIPI



Resuts - Linear Estimation - SDQ



Discussion - Linear Estimation

- **Cognitive Skills:** Strongest predictor of academic performance; one SD increase yields +0.67 (SDQ) to +0.72 (TIPI) points in Maths and +0.42 (SDQ) to +0.45 (TIPI) points in English.
- **Noncognitive Skills:** Focused Behaviour significantly boosts scores (+0.22 in Maths, +0.18 in English); Conscientiousness also impacts significantly (+0.14 in Maths, +0.08 in English).
- **Interaction Effects:** Highly significant negative interactions between cognitive ability and noncognitive skill, which suggests importance for students with lower cognitive abilities.
- **Gender Differences:** Boys perform worse than girls, especially in English (-0.44 points); smaller gap in Maths (-0.12 points).
- **Subject Differences:** Cognitive skills have a stronger impact on Maths; noncognitive skills are more influential in English.

Nonlinear Estimation: Translog P.F.

Equation:

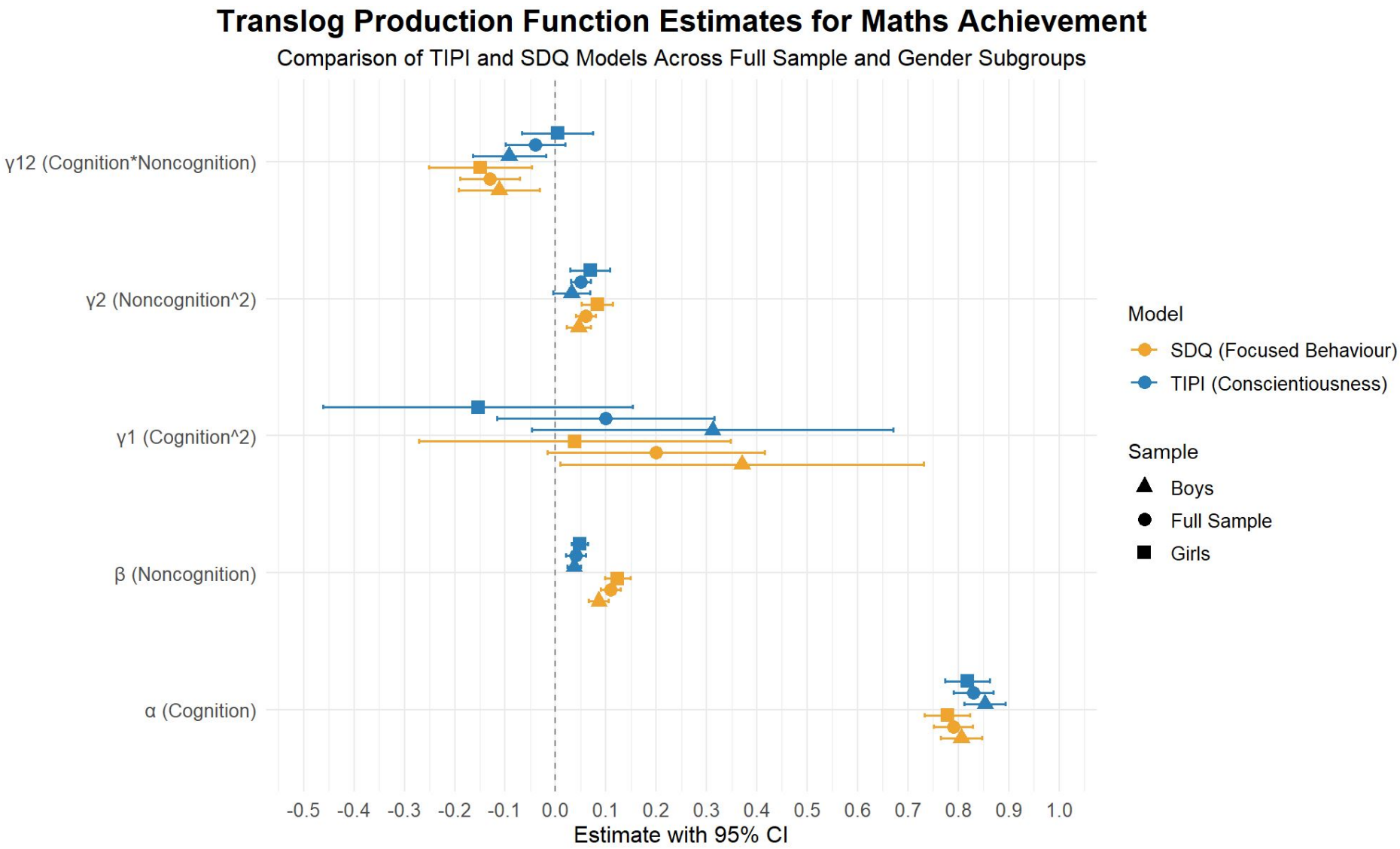
$$Y = AC^{\alpha}N^{\beta}\exp\left\{\frac{1}{2}\gamma_1\left[\ln(C)\right]^2 + \frac{1}{2}\gamma_2\left[\ln(N)\right]^2 + \gamma_{12}\ln(C)\ln(N)\right\}$$

Where:

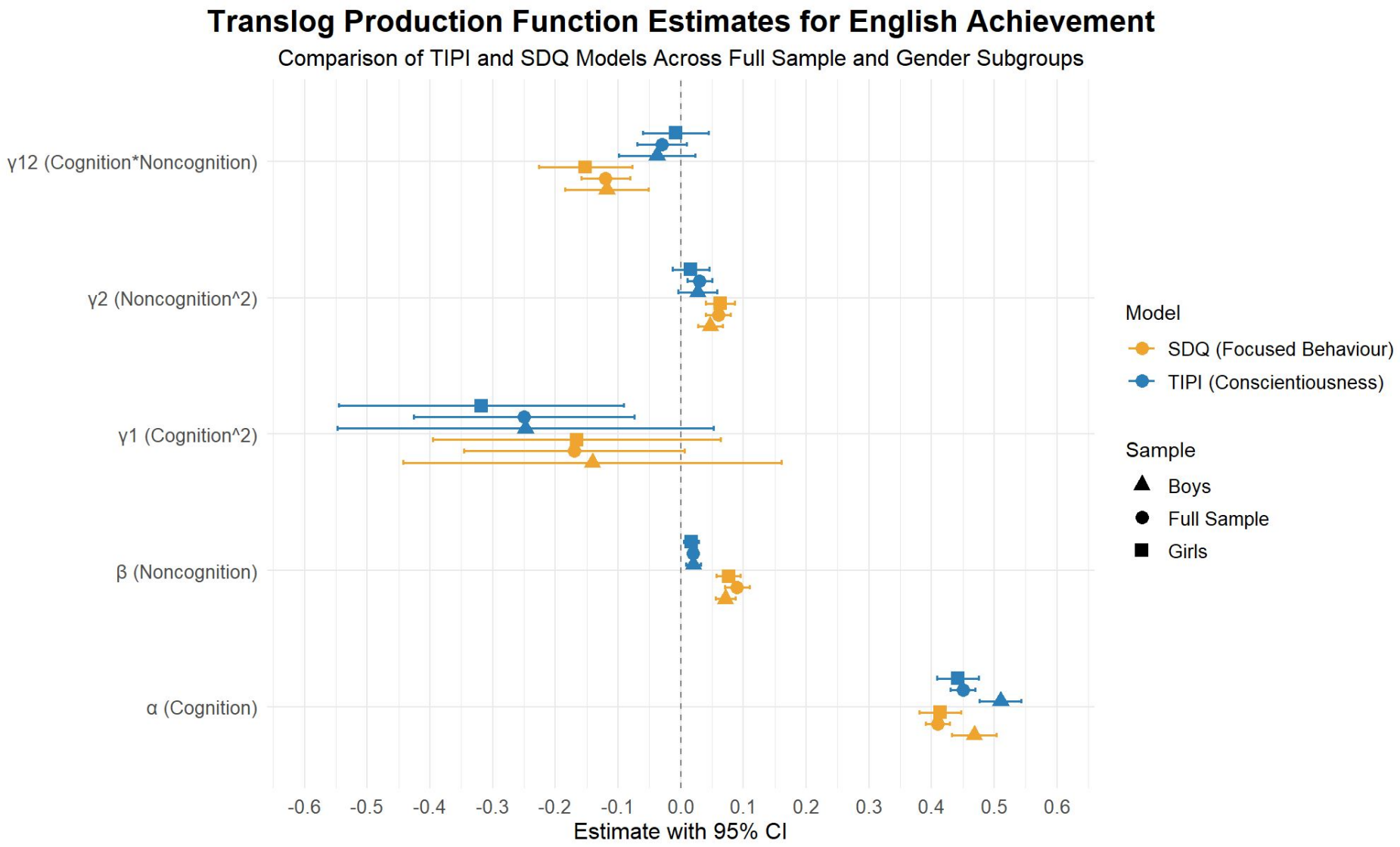
- Y: Output (JC scores in Maths/English), C: Cognitive input (PC with $\mu = 100$ and $\sigma = 15$), N: Noncognitive input (Focused Behaviour and Conscientiousness in the original scales)
- α, β: Output elasticity w.r.t. cognitive and noncognitive inputs
- γ_1, γ_2, γ_{12}: Quadratic and interaction effects (if $\gamma_{12} > 0 =$ complementarity, $\gamma_{12} < 0 =$ substitutability)

The translog PF captures variable elasticities of substitution and complex input interactions; its flexible, second-order approximation, extends beyond traditional models (e.g., Cobb-Douglas); it allows modeling a broader range of input-output relationships.

Results - Nonlinear Estimation - Maths



Results - Nonlinear Estimation - English



Discussion - Nonlinear Estimation

- **Cognitive Skills (α):** Strong influence on performance; $\alpha = 0.79$ (SDQ, Maths) and 0.83 (TIPI, Maths) vs. $\alpha = 0.41$ (SDQ, English) and 0.45 (TIPI, English).
- **Noncognitive Skills (β):** Smaller but significant contributions; $\beta = 0.11$ (Maths, SDQ) vs. $\beta = 0.09$ (English, SDQ); TIPI values lower at 0.04 (Maths) and 0.02 (English).
- **Interaction Effects (γ_{12}):** Negative and significant for SDQ ($\gamma_{12} = -0.13$ for Maths, -0.12 for English) indicating a modest substitutive relationship between cognitive and noncognitive skills.
- **Gender Differences:** Cognitive skills impact varies; girls: $\alpha = 0.778$ (Maths, SDQ), boys: $\alpha = 0.806$ (Maths, SDQ). Noncognitive skills are higher for girls in both subjects.
- **Measurement Tool Impact:** SDQ measures show stronger relationships with outcomes than TIPI, suggesting better relevance for academic performance.

Key Concepts

- **Marginal Products (MPs)** measure the change in output resulting from a one-unit increase in an input, holding other inputs constant. In the Translog model, MPs depend on both the levels of the inputs and their interactions.
- **Output Elasticities (OEs)** represent the responsiveness of output to a change in each input, expressed as a percentage. Translog OEs vary with input levels, reflecting changes in output as inputs vary.
- **Marginal Rate of Technical Substitution (MRTS)** shows how much of one input can be substituted for another while maintaining the same level of output. In the Translog model, MRTS varies with input levels, capturing varying substitutability between inputs.
- **Elasticity of Substitution (ES)** measures the ease of substituting one input for another. For Translog, ES is not constant but depends on the levels of inputs.

Definitions

Results - Nonlinear Estimation

	Maths			English		
Estimate	**Full**	**Boys**	**Girls**	**Full**	**Boys**	**Girls**
TIPI Model						
MP (Cognition)	0.08	0.080	0.078	0.05	0.049	0.047
MP (Conscientiousness)	0.08	0.073	0.091	0.05	0.041	0.035
OE (α Cognition)	0.83	0.859	0.820	0.45	0.506	0.447
OE (β Conscientiousness)	0.04	0.036	0.048	0.02	0.019	0.017
EoS	-0.30	-1.941	0.853	0.16	-0.953	1.257
MRTS	0.93	1.102	0.858	0.89	1.217	1.342
SDQ Model						
MP (Cognition)	0.07	0.076	0.074	0.04	0.045	0.043
MP (Focused Behaviour)	0.12	0.103	0.140	0.11	0.088	0.095
OE (α Cognition)	0.79	0.813	0.778	0.41	0.466	0.416
OE (β Focused Behaviour)	0.11	0.084	0.125	0.09	0.069	0.078
EoS	-0.26	-0.470	-0.092	0.02	-0.348	-0.722
MRTS	0.61	0.733	0.530	0.38	0.513	0.455

Note: MP = Marginal Product, OE = Output Elasticity, EoS = Elasticity of Substitution, MRTS = Marginal Rate of Technical Substitution.

Discussion - Nonlinear Estimation

- **Higher Marginal Products (MPs):** Both cognitive and noncognitive skills yield greater returns in Maths than in English.
- **Output Elasticities (OEs):** Cognitive skills, particularly in Maths, have a more substantial impact on academic outcomes compared to noncognitive skills.
- **Elasticity of Substitution:** Varies widely across models, indicating that substitutability between skills is context-dependent, influenced by subject matter and student characteristics.
- **Marginal Rate of Technical Substitution (MRTS):** Generally less than 1, suggesting multiple noncognitive skill units are needed to substitute for one cognitive skill unit to maintain performance.
- **Decreasing Returns to Scale:** The sum of coefficients $(\alpha + \beta)$ is consistently less than 1, indicating diminishing returns in educational production.

Conclusion

- **Focus of Study:** Examined interactions of cognitive and noncognitive skills on academic achievement in Maths and English, highlighting gender differences.
- **Cognitive Skills:** Primary predictor of performance; stronger impact in Maths compared to English.
- **Noncognitive Skills:** Significant but smaller effects when compared to cognitive ability.
- **Gender Differences:** Boys showed higher cognitive output elasticities; girls had stronger noncognitive effects, particularly in Maths.
- **Model Insights:** The translog model revealed variable elasticity of substitution, indicating a shifting importance of skills as students progress.
- **Policy Implications:** Interventions should target both cognitive and noncognitive skills, tailored to specific subjects and gender needs to enhance academic outcomes.

Conclusion

Thank you so much.
Any questions or suggestions?
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Descriptive Statistics - Main Variables

Table: Descriptive Statistics - Main Variables

Variable	Mean	Std. Dev.	Min	Max	N
Dependent variables					
Maths points (Junior Cert)	9.60	1.74	2.00	12.00	5631
English points (Junior Cert)	10.15	1.34	5.00	12.00	5631
Independent variables: Cognition					
Drumcondra Verbal Reasoning (% of correct answers)	64.89	21.92	0.00	100.00	5631
Drumcondra Numerical Ability (% of correct answers)	55.05	22.53	0.00	100.00	5631
Matrices (BSA)	116.68	18.03	10.00	161.00	5631
Cognitive ability 1	0.14	1.33	-4.25	3.32	5631
Cognitive ability 2	100.00	15.00	36.25	136.40	5631
Independent variables: Noncognition (SDQ scale)					
Emotional resilience	8.29	1.87	0.00	10.00	5631
Good conduct	8.97	1.31	0.00	10.00	5631
Focused behaviour	7.56	2.26	0.00	10.00	5631
Positive peer relationships	8.96	1.41	0.00	10.00	5631
Independent variables: Noncognition (TIPI scale)					
Agreeable	5.01	1.95	0.50	7.00	5631
Conscientious	4.33	2.07	0.50	7.00	5631
Emotional stability	4.40	1.99	0.50	7.00	5631
Extravert	3.98	1.98	0.50	7.00	5629
Openness	4.73	1.83	0.50	7.00	5627

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Descriptive Statistics - Control Variables

Table: Descriptive Statistics - Control Variables

Variable	Mean	Std. Dev.	Min	Max	N
Controls (SES characteristics)					
Gender (Male = 1)	0.49	0.50	0.00	1.00	5468
Primary caregiver education level	3.97	1.24	1.00	6.00	5631
Secondary caregiver education level	3.86	1.36	1.00	6.00	4440
Income quintile (equivalized)	3.33	1.39	1.00	5.00	5241
Controls (School characteristics, binary)					
DEIS (Delivering Equality of Opportunity In Schools)	0.12	0.33	0.00	1.00	5452
Fee-paying	0.10	0.30	0.00	1.00	5452
Mixed-school	0.54	0.50	0.00	1.00	5317

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Notes I

- For the analysis, I used the Junior Certificate Overall Performance Scale (OPS), which converts letter grades from different exam levels to a standardized 12-point numerical scale. This scale has been validated in previous research by Nick Sofroniou, Gerry Shiel and Judith Cosgrove (2000), and it provides a comprehensive measure that accounts for both grade and exam level.
- TIPI scale scores on a 1-7 scale in intervals of 0.5, and the original SDQ scales, ranging from 0 to 10, have been inverted (higher scores typically indicate more problems on the original SDQ scale).
- "Cognitive ability 1" was used in the first part of the production function estimation and was standardized to have mean = 0 and standard deviation = 1. "Cognitive ability 2" is to be used in the second part of the analysis as a measure of cognition in non-linear production function estimation, with a mean of 100 and standard deviation = 15 as is standard in the literature.
- Education levels are coded from 1 (Primary or less) to 6 (Postgraduate/Higher degree) in the Growing Up in Ireland caregiver questionnaire. The mean values for both primary (3.97) and secondary (3.86) caregivers indicate an average education level between Leaving Certificate and Diploma/Certificate, suggesting a higher proportion of educated caregivers in the sample.
- Income is reported in quintiles, where 1 represents the lowest 20% and 5 the highest 20% of incomes. The mean of 3.33 suggests that the sample is slightly skewed towards higher income levels, with families on average being just above the median income quintile.
- The sample includes 12% DEIS schools (schools in disadvantaged areas), 10% fee-paying schools, and 54% mixed-gender schools. This suggests a diverse range of school types, with a notably high proportion of fee-paying schools and a relatively low proportion of DEIS schools.

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Notes II

Table: Junior Certificate Overall Performance Scale (OPS)

Higher Level	Ordinary Level	Foundation Level	OPS Score
A			12
B			11
C			10
D	A		9
E	B		8
F	C		7
	D	A	6
	E	B	5
	F	C	4
		D	3
		E	2
		F	1

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Definitions

$$MP_C = A\alpha C^{\alpha-1} N_0^{\beta} \exp\left\{\frac{1}{2}\gamma_1 [\ln(C)]^2 + \frac{1}{2}\gamma_2 [\ln(N_0)]^2 + \gamma_{12}\ln(C)\ln(N_0)\right\}\left[\gamma_1 \ln(C)\frac{1}{C} + \gamma_{12}\frac{\ln(N_0)}{C}\right] \tag{1}$$

$$MP_N = A\beta C_0^{\alpha} N^{\beta-1} \exp\left\{\frac{1}{2}\gamma_1 [\ln(C_0)]^2 + \frac{1}{2}\gamma_2 [\ln(N)]^2 + \gamma_{12}\ln(C_0)\ln(N)\right\}\left[\gamma_2 \ln(N)\frac{1}{N} + \gamma_{12}\frac{\ln(C_0)}{N}\right] \tag{2}$$

$$OE_C = \left.\frac{\partial \ln(Y)}{\partial \ln(C)}\right|_{N=N_0} = \alpha + \gamma_1 \ln(C) + \gamma_{12}\ln(N_0) \tag{3}$$

$$OE_N = \left.\frac{\partial \ln(Y)}{\partial \ln(N)}\right|_{C=C_0} = \beta + \gamma_2 \ln(N) + \gamma_{12}\ln(C_0) \tag{4}$$

$$MRTS_{CN} = \frac{\alpha + \gamma_1 \ln(C) + \gamma_{12}\ln(N)}{\beta + \gamma_2 \ln(N) + \gamma_{12}\ln(C)} \cdot \frac{N}{C} \tag{5}$$

$$EoS = 2 - \frac{\gamma_1}{OE_C} + \frac{\gamma_{12}}{OE_N} + \frac{\gamma_{12}}{OE_C} - \frac{\gamma_2}{OE_N} \tag{6}$$

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